

Embodied artificial intelligence through free energy minimization

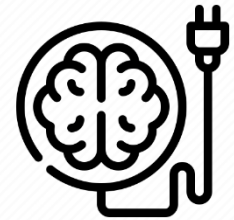
Wouter Kouw
EAISI AI Café
September 19th 2024



Dangerous jobs



Embodied Artificial Intelligence



~20 Watt

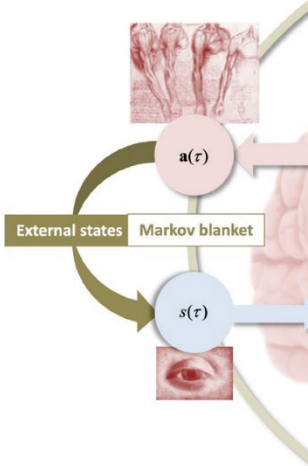
Hafner, DayDreamer; <https://www.youtube.com/watch?v=xAXvVTgqr0>

~10-20 MegaWatt

Free energy minimization



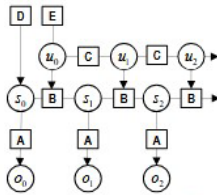
Automatic Bayesian Inference through Reactive Message Passing



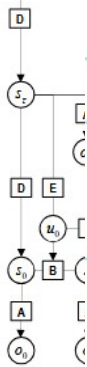
Parametric depth

$$\begin{aligned}
 P(a_t | s_{t-1}, a) &= \text{Cat}(\mathbf{A}) \\
 P(s_{t+1} | s_t, u_t, \delta) &= \text{Cat}(\mathbf{B}) \\
 P(u_{t+1} | u_t, c) &= \text{Cat}(\mathbf{C}) \\
 P(s_t | a) &= \text{Cat}(\mathbf{D}) \\
 P(u_t | e) &= \text{Cat}(\mathbf{E}) \\
 P(\mathbf{A}) &= \text{Dir}(a), \dots \\
 \mathbb{E}[P(\mathbf{A})] &=: \mu(a) = a/a_0, a_0 = \sum_i a_i \\
 \mathbb{E}[\ln P(\mathbf{A})] &=: \phi(a) = \psi(a) - \psi(a_0) \\
 \ell(a) &= \ln(a) \\
 \sigma(a) &=: \mu(e^a)
 \end{aligned}$$

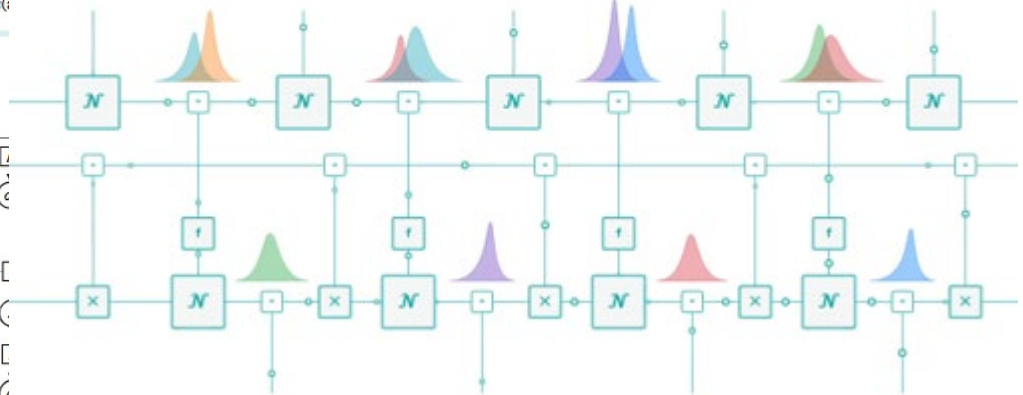
$$\begin{aligned}
 P(u_{t+1} | u_t) &= \text{Cat}(\mathbf{C}) \\
 P(u_{t+1} | c) &= \text{Cat}(\mathbf{C}) \\
 \mathbf{C} &= \pi \odot \sigma(\cdot) \\
 G_i &= \sum_s \mathbf{o}_{t+1}^s \\
 \mathbf{o}_{t+1}^s &= \mu(\mathbf{a}^s) \odot \\
 s_{t+1}^k &= \mu(\mathbf{b}^k | s) \\
 \mathbf{H}^s &= \mathbf{1} \odot (\mu(\cdot)
 \end{aligned}$$



Temporal depth



Hierarchical depth



Factorial depth

Free energy minimizing agents

$$\begin{pmatrix} \mu_{k-1} \\ \Lambda_{k-1} \\ \alpha_{k-1} \\ \beta_{k-1} \end{pmatrix}$$

